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Research Paper

## IS-MRAS With On-Line Adaptation Parameters Based on Type-2 Fuzzy LOGIC for Sensorless Control of IM

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**Abstract:** This paper suggests novel sensorless speed estimation for an induction motor (IM) based on a stator current model reference adaptive system (IS-MRAS) scheme. The IS-MRAS scheme uses the error between the reference and estimated stator current vectors and the rotor speed. Observing rotor flux and the speed estimating using the conventional MRAS technique is confronted with certain problems related to the presence of the pure integrator and the rotor resistance causing offsets at low speeds, as proved by the most recent publications. These offsets are disastrous in sensorless control since these signals are no longer suitable to calculate of park angle ( $\theta_s$ ). This paper discusses the new MRAS approach (IS-MRAS) for on-line identification of the rotor resistance suitable for compensating offsets and solving problems of ordinary MRAS at low speed. This new MRAS approach used to estimate the components of the rotor flux and rotor speed without using the voltage model with on-line Setting parameters ( $K_p$ ,  $K_1$ ) based on Type-2 fuzzy Logic. The results of the simulation and the experimental results are presented and show the effectiveness of the proposed technique.

Keywords: Induction Motor, IS-MRAS, Type-2 Fuzzy logic, Sensorless Control.

## 1 Introduction

THE asynchronous machine, by its construction, is the most robust machine and least costly. The advances made in control and the considerable technological advances in both the power electronics and microelectronics have made it possible to install the powerful controls of this machine, making it a dreadful concurrent in the sectors of variable speed.

However, many problems remain, since the variation of the parameters of the machine, the presence of the mechanical sensor and the degraded operation are all difficulties that have emulated the eagerness of the

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researchers, as proved by the ever-increasing number of publications that study the subject, [1-22].

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Control of induction machine (IM) requires the installation of an incremental encoder for the speed measure. The use of this encoder results in an additional cost which may be greater than that of the machine and especially in the case of low power machines. However, the reliability of the system decreases because of this fragile device which in turn requires special maintenance.

That is why the idea of eliminating the incremental encoder has arisen and that the research on the sensorless control of the asynchronous machine is begun and is continuously expanding.

Several strategies have been proposed in the literature to achieve this object. A large part of the proposed methods is based on observers depending on the machine model.

Unfortunately, these techniques fail to replace the incremental encoder in the low-speed range and also during the presence of disturbances such as the load application; this consists of the essential problem of these techniques. Other research is based on the contribution of artificial intelligence to improve machine sensorless control. Among them, we can

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highlight methods by sliding mode [4, 5], using a new concept of stator resistance [19], and many adaptive methods (MRAS) have been proposed such as [1-3], [6, 7], [9-11], [21, 22]. However, rotor flux MRAS first introduced by Schauder [2], the MRAS strategy remains the most popular, and a lot of effort has been focused on improving its performance, the results obtained by these authors confirm, indeed, the disadvantages of this technique which are the sensitivity to the variation of the parameters, in particular to the rotor resistance, and pure integration problems, which limit its performance at low and zero speed regions of operation.

In this paper, we propose a new MRAS approach with the on-line adaptation of the speed estimation mechanism parameters, moreover, we propose the online estimation of the rotor resistance.

The type-2 fuzzy logic was used to supervise the variations of Kp and  $K_i$  of the speed estimator.

The Novelty in this paper is the elimination of the voltage model, because the conventional MRAS technique is confronted with certain problems related to the presence of the pure integrator in the voltage model causing offsets at low speeds, this offsets are disastrous in control since these signals are no longer suitable to calculate of park angle ( $\theta_s$ ).

The validity of the proposed method is verified using simulation and experimentation. Moreover, the sensorless control of the asynchronous machine associated with the static converter presents several difficulties in terms of performance, in this context the use of type-2 fuzzy logic constitutes an interesting alternative for improving the performance of the new approach of MRAS observer in low speed.

#### 2 Asynchronous Motor Model

We consider two mathematical models, the first is used to realize the control vector and the second is used to synthesize observer.

Model related to the rotating field (dq-coordinates):

$$\begin{cases} \frac{di_{sd}}{dt} = -\frac{R}{\sigma L_s} i_{sd} + \omega_s i_{sq} + \frac{M}{\sigma L_s L_r} \left(\frac{1}{T_r} \varphi_{rd} + \omega \varphi_{rq}\right) + \frac{1}{\sigma L_s} V_{sd} \\ \frac{di_{sq}}{dt} = -\frac{R}{\sigma L_s} i_{sq} - \omega_s i_{sd} + \frac{M}{\sigma L_s L_r} \left(\frac{1}{T_r} \varphi_{rq} - \omega \varphi_{rd}\right) + \frac{1}{\sigma L_s} V_{sq} \\ \frac{d\varphi_{rd}}{dt} = \frac{M}{T_r} i_{sd} - \frac{1}{T_r} \varphi_{rd} + (\omega_s - \omega) \varphi_{rq} \\ \frac{d\varphi_{rq}}{dt} = \frac{M}{T_r} i_{sq} - \frac{1}{T_r} \varphi_{rq} - (\omega_s - \omega) \varphi_{rd} \\ T_e = \frac{P.M}{L_r} (i_{sq} \varphi_{rd} - i_{sd} \varphi_{rq}) \end{cases}$$
(1)

In the stationary reference frame ( $\alpha\beta$ -coordinates), the dynamic model of a 3-phase induction motor can be described as

$$\left| \frac{d\varphi_{r\alpha}}{dt} = \frac{L_r}{M} \left( V_{s\alpha} - R_s i_{s\alpha} - \sigma L_s \frac{di_{s\alpha}}{dt} \right) \\ \frac{d\varphi_{r\beta}}{dt} = \frac{L_r}{M} \left( V_{s\beta} - R_s i_{s\beta} - \sigma L_s \frac{di_{s\beta}}{dt} \right) \\ \frac{d\varphi_{r\alpha}}{dt} = \frac{M}{T_r} i_{s\alpha} - \frac{1}{T_r} \varphi_{r\alpha} - \omega \varphi_{r\beta} \\ \frac{d\varphi_{r\beta}}{dt} = \frac{M}{T_r} i_{s\beta} - \frac{1}{T_r} \varphi_{r\beta} + \omega \varphi_{r\alpha}$$
(2)

where

$$\sigma = 1 - \frac{M^2}{L_s L_r}, \ \sigma = R_r - \frac{M^2}{L_r^2}, \ T_r = \frac{L_r}{R_r}$$

where  $V_s$  is the stator voltage,  $V_r$  is the rotor voltage,  $R_s$  is the stator resistance,  $R_r$  is the rotor resistance,  $\omega$  is the electrical angular frequency,  $\varphi_s$  is the stator flux,  $\varphi_r$  is the rotor flux power and  $L_s$ , M, and  $L_r$  are the stators, magnetizing, and rotor inductances, respectively.

#### 3 Vector Control

To test the proposed approach, we use indirect vector control as shown in Fig 2. We take  $V_{sd}$  and  $V_{sq}$  as control variables. In this context and for  $\varphi_{rq} = 0$ , the equations system (1) becomes:

$$V_{sd} = \sigma L_s \frac{di_{sd}}{dt} + Ri_{sd} - \omega_s \sigma L_s i_{sq} + \frac{M}{L_r} \left(\frac{1}{T_r} \varphi_{rd}\right)$$
(3)

$$V_{sq} = \sigma L_s \frac{di_{sq}}{dt} + \mathbf{R}.i_{sq} + \omega_s \sigma L_s i_{sd} + \frac{M}{L_r} (\omega \varphi_{rd})$$
(4)

$$\frac{M}{T_r}i_{sq} = (\omega_s - \omega)\varphi_{rd}$$
(5)

$$T_r \frac{d\varphi_{rd}}{dt} + \varphi_{rd} = M \, i_{sd} \tag{6}$$

$$C_e = \frac{3}{2} \frac{pM}{L_r} \left( \varphi_{rd} i_{sq} \right) \tag{7}$$

where  $C_e$  is the electromagnetic torque.

Expression (6) shows that the rotor flux evolution follows the stator current, furthermore, the torque of (7) is similar to that to DC motor because  $i_{sd}$  and  $i_{sq}$  are continuous components. It can be said that with the field orientation, the torque control becomes linear and adjustable by acting on  $i_{sq}$  when the flux  $\varphi_{dr}$  is kept constant. If the flux  $\varphi_{rd}$  is replaced by the reference flux  $\varphi_r^*$ , the developed torque given by (7) can be rewritten as follows:

$$C_e = k \varphi_r^* i_{sq} \tag{8}$$

where  $k = \frac{3}{2} \frac{pM}{L_r}$  and  $\varphi_r^*$  is the rotor flux reference.

From (5), we deduce the Park angle:

$$\theta_{s} = \int \omega_{s} dt = \int \left( \omega + \frac{Mi_{sq}}{T_{r} \varphi_{rd}} \right) dt$$
(9)

The decoupling by compensation as follows:

$$V_{sd}^* = V_{sd} + e_{sd} \tag{10}$$

$$V_{sq}^* = V_{sq} + e_{sq} \tag{11}$$

where

$$e_{sd} = \omega_s \sigma L_s i_{sq} - \frac{M}{T_r L_r}$$
(12)

$$e_{sq} = -\omega_s \sigma L_s i_{sd} - \omega \frac{M}{L_r} \varphi^*$$
<sup>(13)</sup>

$$V_{sd}^* = \sigma L_s \frac{di_{sd}}{dt} + Ri_{sd} \tag{14}$$

$$V_{sq}^* = \sigma L_s \frac{di_{sq}}{dt} + Ri_{sq}$$
(15)

From new components  $V_{sd}^*$  and  $V_{sq}^*$ , we deduce the control components  $V_{sd}$  and  $V_{sq}$ .

## 4 Classical MRAS Observer

The MRAS observer analyzed two independent equations for the derivative time of the rotor flux vector, obtained from (2). They are usually referred to as the "voltage model" called reference model and "current model" called adjustable model and they are given, respectively, by

$$\begin{cases} \frac{d\varphi_{r\alpha}}{dt} = \frac{L_r}{M} \left( V_{s\alpha} - R_s i_{s\alpha} - \sigma L_s \frac{di_{s\alpha}}{dt} \right) \\ \frac{d\varphi_{r\beta}}{dt} = \frac{L_r}{M} \left( V_{s\beta} - R_s i_{s\beta} - \sigma L_s \frac{di_{s\beta}}{dt} \right) \end{cases}$$
(16)

and we propose the following current reference model:

$$\begin{cases} \frac{d\varphi_{r\alpha}}{dt} = \frac{M}{T_r} i_{s\alpha} - \frac{1}{T_r} \varphi_{r\alpha} - \omega \varphi_{r\beta} \\ \frac{d\varphi_{r\beta}}{dt} = \frac{M}{T_r} i_{s\beta} - \frac{1}{T_r} \varphi_{r\beta} + \omega \varphi_{r\alpha} \end{cases}$$
(17)

the model (17) can be written in an adjustable form:

$$\begin{cases} \frac{d\hat{\varphi}_{r\alpha}}{dt} = \frac{M}{T_r} i_{s\alpha} - \frac{1}{T_r} \hat{\varphi}_{r\alpha} - \hat{\omega} \hat{\varphi}_{r\beta} \\ \frac{d\hat{\varphi}_{r\beta}}{dt} = \frac{M}{T_r} i_{s\beta} - \frac{1}{T_r} \hat{\varphi}_{r\beta} + \hat{\omega} \hat{\varphi}_{r\alpha} \end{cases}$$
(18)

where  $\hat{\varphi}_r$  is the estimated rotor flux and  $\hat{\omega}$  is estimated rotor speed.

The dynamic equation of the estimation error  $\varepsilon_{\alpha\beta}$  is obtained by subtracting (17) and (18).

$$\begin{cases} \frac{d\varepsilon_{\alpha}}{dt} = -\frac{1}{T_{r}}\varepsilon_{\alpha} - \omega\varepsilon_{\beta} - (\omega - \hat{\omega})\hat{\varphi}_{r\beta} \\ \frac{d\varepsilon_{\beta}}{dt} = -\frac{1}{T_{r}}\varepsilon_{\beta} + \omega\varepsilon_{\alpha} + (\omega - \hat{\omega})\hat{\varphi}_{r\alpha} \end{cases}$$
(19)  
where  $\varepsilon_{\alpha\beta} = \begin{bmatrix} \varphi_{r\alpha} - \hat{\varphi}_{r\alpha} \\ \varphi_{r\beta} - \hat{\varphi}_{r\beta} \end{bmatrix}$ .

For the correctness of the parameter technique, it must be ensured that the system (19) is stable. It naturally requires the error ( $\varepsilon_{\alpha\beta}$ ) tends to be zero. The stability of this algorithm is studied, using the hyper-stability Popov criterion.

The system (19) can be written in the following matrix form:

$$\frac{d\varepsilon_{\alpha\beta}}{dt} = A_{\omega}\varepsilon_{\alpha\beta} - C_{\omega}$$
<sup>(20)</sup>

where

$$A_{\omega} = \begin{bmatrix} \frac{-1}{T_r} & -\omega \\ \omega & \frac{-1}{T_r} \end{bmatrix} \text{ and } C_{\omega} = \begin{bmatrix} 0 & (\omega - \hat{\omega}) \cdot \hat{\Phi}_{r\beta_{-}aj} \\ -(\omega - \hat{\omega}) \cdot \hat{\Phi}_{r\alpha_{-}aj} & 0 \end{bmatrix}$$

We consider the adaptation law proposed by [11]:

$$\hat{\omega} = f_2(\varepsilon) + \int_0^t f_1(\varepsilon) d\tau$$
(21)

The criterion of Popov requires that:

$$\int_{0}^{t_{1}} \varepsilon^{T} C_{\omega} dt \ge -\gamma_{0}^{2}; \forall t_{1} \ge 0$$
(22)

where  $\gamma_0^2$  is a positive constant. The solution of (22) proposed by [10] is:

$$\begin{cases} f_1 = K_i \left( \varphi_{r\beta} \cdot \hat{\varphi}_{r\alpha} - \varphi_{r\alpha f} \cdot \hat{\varphi}_{r\beta} \right) \\ f_2 = K_p \left( \varphi_{r\beta} \cdot \hat{\varphi}_{r\alpha} - \varphi_{r\alpha f} \cdot \hat{\varphi}_{r\beta} \right) \end{cases}$$
(23)

By replacing (23) in (21), we obtain the speed estimation:

$$\hat{\omega} = K_{p} \left( \varphi_{r\beta} . \hat{\varphi}_{r\alpha} - \varphi_{r\alpha f} . \hat{\varphi}_{r\beta} \right) + K_{i} \int_{0}^{t} \left( \varphi_{r\beta} . \hat{\varphi}_{r\alpha} - \varphi_{r\alpha f} . \hat{\varphi}_{r\beta} \right) dt$$
(24)

where  $K_p$  and  $K_i$  are positive gains.

However, the main problem of the classical MRAS observer is its poor estimation at low speeds [6], [9-11], [21, 23]. That is why we present a new MRAS speed observer in the following paragraph.

# 5 Stator Current Model Reference Adaptive System (IS-MRAS)

The proposed MRAS is using the current model only.

The idea is to eliminate the influence of the voltage model (16) because this model presents a pure integration of the rotor flux, so at low speed ( $\omega \approx 0$ ) we can have the offset problem. Fig. 1 shows the block diagram of the proposed new approach MRAS.

From the system (2), we propose the following current reference model:

$$\begin{cases} \frac{d\varphi_{r\alpha}}{dt} = \frac{M}{T_r} i_{s\alpha} - \frac{1}{T_r} \varphi_{r\alpha} - \omega \varphi_{r\beta} \\ \frac{d\varphi_{r\beta}}{dt} = \frac{M}{T_r} i_{s\beta} - \frac{1}{T_r} \varphi_{r\beta} + \omega \varphi_{r\alpha} \end{cases}$$
(25)

If  $\omega = \omega_{ref}$  and  $T_r = \hat{T}_r$  then flux  $\varphi_{r\alpha}$  and  $\varphi_{r\beta}$  are considered as references. The proposed model (25) becomes:

$$\begin{cases} \frac{d\varphi_{r\alpha}}{dt} = \frac{M}{\hat{T}_{r}} i_{s\alpha} - \frac{1}{\hat{T}_{r}} \varphi_{r\alpha} - \omega_{ref} \varphi_{r\beta} \\ \frac{d\varphi_{r\beta}}{dt} = \frac{M}{\hat{T}_{r}} i_{s\beta} - \frac{1}{\hat{T}_{r}} \varphi_{r\beta} + \omega_{ref} \varphi_{r\alpha} \end{cases}$$
(26)

If  $\omega = \hat{\omega}$  and  $T_r = \hat{T}_r$ , then flux  $\varphi_{r\alpha}$  and  $\varphi_{r\beta}$  are considered as estimates and model (25) becomes:

$$\begin{cases} \frac{d\hat{\varphi}_{r\alpha}}{dt} = \frac{M}{\hat{T}_{r}} i_{s\alpha} - \frac{1}{\hat{T}_{r}} \hat{\varphi}_{r\alpha} - \hat{\omega} \hat{\varphi}_{r\beta} \\ \frac{d\hat{\varphi}_{r\beta}}{dt} = \frac{M}{\hat{T}_{r}} i_{s\beta} - \frac{1}{\hat{T}_{r}} \hat{\varphi}_{r\beta} + \hat{\omega} \hat{\varphi}_{r\alpha} \end{cases}$$
(27)

With (26) and (27), we can establish the error dynamics:

$$e = \begin{bmatrix} e_{r\alpha} \\ e_{r\beta} \end{bmatrix} = \begin{bmatrix} \varphi_{r\alpha} - \hat{\varphi}_{r\alpha} \\ \varphi_{r\beta} - \hat{\varphi}_{r\beta} \end{bmatrix}$$
(28)

To estimate of rotor resistance, we propose the following algorithm:

$$\dot{\theta}_{ref} - \dot{\theta} = -\frac{M}{L_r \cdot \varphi_r} R_r \dot{i}_{sq} + \frac{M}{L_r \hat{\varphi}_r} \hat{R}_r \dot{i}_{sq}$$
(29)

If we pose  $\omega_{ref} - \hat{\omega} = \dot{\theta}_{ref} - \dot{\theta} = \dot{e}_{\omega}$ , we obtain:

$$\dot{e}_{\omega} = \mu \left( \frac{R_r}{\varphi_r} - \frac{\hat{R}_r}{\hat{\varphi}_r} \right)$$
(30)

where 
$$\hat{\varphi}_r = \sqrt{\hat{\varphi}_{r\alpha}^2 + \hat{\varphi}_{r\beta}^2}$$
,  $\varphi_r = \sqrt{\varphi_{r\alpha}^2 + \varphi_{r\beta}^2}$ ,  $\mu = -\frac{M}{L_r} i_{sq}$ ,

and  $i_{sq}$  is the torque current.

The error e can be written in the following complex form:

$$\overline{e} = e_{r\alpha} + je_{r\beta} \tag{31}$$

And the system (26) can be written in the following complex form:

$$\frac{M}{T_r}\overline{i_s} = \frac{d\overline{\varphi}_r}{dt} + \frac{\overline{\varphi}_r}{\hat{T}_r} - j\omega\overline{\varphi}_r$$
(32)

If  $\omega = \omega_{ref}$ , we write:



Fig. 1 Block diagram of the proposed MRAS.

$$\frac{M}{T_r}\bar{i}_s = \frac{d\bar{\varphi}_r}{dt} + \frac{\bar{\varphi}_r}{\hat{T}_r} - j\omega_{ref}\bar{\varphi}_r$$
(33)

and if  $\omega = \hat{\omega}$ , we write:

$$\frac{M}{T_r}\overline{i}_s = \frac{d\overline{\varphi}_r}{dt} + \frac{\overline{\varphi}_r}{\hat{T}_r} - j\hat{\omega}\overline{\varphi}_r$$
(34)

Let us make now the subtraction between (34) and (33), one obtains:

$$0 = \dot{\overline{e}} + \frac{1}{\hat{T}_{r}}\overline{\overline{e}} - j\omega_{ref}\overline{\varphi}_{r} + j\hat{\omega}\overline{\varphi}_{r}$$
$$= \dot{\overline{e}} + \frac{1}{\hat{T}_{r}}\overline{\overline{e}} - j\omega_{ref}\overline{\varphi}_{r} + j\hat{\omega}\overline{\varphi}_{r} + j\omega_{ref}\overline{\varphi}_{r} - j\omega_{ref}\overline{\varphi}_{r}$$
$$= \dot{\overline{e}} + \left(\frac{1}{\hat{T}_{r}} - j\omega_{ref}\right)\overline{\overline{e}} - j\left(\omega_{ref} - \hat{\omega}\right)\overline{\varphi}_{r}$$
(35)

This gives:

$$\dot{\overline{e}} = \overline{A}\overline{e} + \overline{W}$$
(36)  
where  $\overline{A} = -\left(\frac{1}{\hat{T}_{r}} - j\omega_{ref}\right)$  with  $A = \begin{bmatrix} -\frac{1}{\hat{T}_{r}} & -\omega_{ref} \\ \omega_{ref} & -\frac{1}{\hat{T}_{r}} \end{bmatrix}$ .  
 $\overline{W} = j\left(\omega_{ref} - \hat{\omega}\right)\overline{\varphi}_{r} = j\mu\left(\frac{R_{r}}{\varphi_{r}} - \frac{\hat{R}_{r}}{\hat{\varphi}_{r}}\right)\overline{\varphi}$ 
(37)

and

$$W = \Delta \omega \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \hat{\varphi}_{r\alpha} \\ \hat{\varphi}_{r\beta} \end{bmatrix}$$
$$= \mu \left( \frac{R_r}{\varphi_r} - \frac{\hat{R}_r}{\hat{\varphi}_r} \right) \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \hat{\varphi}_{r\alpha} \\ \hat{\varphi}_{r\beta} \end{bmatrix}$$
(38)

It is necessary to ensure the convergence of the estimation error towards zero, so we have to make sure that the system (34) is stable, the stability of this algorithm is studied using the hyperstability Popov criterion. Indeed, the derivation of the error is composed of two terms. The first is linear and the second is nonlinear.

We define the following Lyapunov function:

$$V = e^{T} e + \frac{\left(\omega_{ref} - \hat{\omega}\right)^{2}}{2\gamma} \ge 0$$
(39)

where  $\gamma$  is a positive constant.

The function given in (34) is globally negative definite. Thus,  $\dot{V} < 0 \quad \forall \hat{\omega}$ .

The time derivative of the Lyapunov function becomes:

$$\dot{V} = \frac{1}{2} \left( \dot{e}^{T} e + e^{T} \dot{e} \right) + \frac{1}{\gamma} \Delta \omega \frac{d \left( \Delta \omega \right)}{dt} + \frac{e_{\omega}^{2}}{2}$$

Let us replace <sup>e</sup> by its value:

$$\dot{V} = \frac{1}{2} \left( \left( Ae + \overline{W} \right)^T e + e^T \left( Ae + \overline{W} \right) \right) + \frac{\Delta \omega}{\gamma} \frac{d \left( \Delta \omega \right)}{dt}$$

$$= \frac{1}{2} \left( e^T A^T e + \overline{W}^T e + e^T Ae + e^T \overline{W} \right) + \frac{\Delta \omega}{\gamma} \frac{d \left( \Delta \omega \right)}{dt}$$

$$= \frac{1}{2} \left( e^T \left( A^T + A \right) e \right) + e^T \overline{W} + \frac{\Delta \omega}{\gamma} \frac{d \left( \Delta \omega \right)}{dt} + \frac{de_{\omega}}{dt} e_{\omega}$$

$$= Q + P$$
(40)

Where

The first term of (40) is negative. If P = 0, then:

$$e^{T}\overline{W} = -\frac{\Delta\omega}{\gamma} \frac{d(\Delta\omega)}{dt}$$
(41)

$$\hat{R}_r = R_r \frac{\varphi_r}{\varphi_r} \tag{42}$$

where

$$e^{T}\overline{W} = \Delta\omega \begin{bmatrix} \varphi_{r\alpha} - \hat{\varphi}_{r\alpha} & \varphi_{r\beta} - \hat{\varphi}_{r\beta} \end{bmatrix} \begin{bmatrix} \hat{\varphi}_{r\beta} \\ -\hat{\varphi}_{r\alpha} \end{bmatrix}$$
$$= \Delta\omega \Big(\varphi_{r\alpha}\hat{\varphi}_{r\beta} - \varphi_{r\beta}\hat{\varphi}_{r\alpha}\Big)$$
(43)

We replace (43) into (41), we obtain:

$$\frac{d\hat{\omega}}{dt} = \gamma \left( \varphi_{r\alpha} \hat{\varphi}_{r\beta} - \varphi_{r\beta} \hat{\varphi}_{r\alpha} \right) 
\hat{\omega} = \gamma \int \left( \varphi_{r\alpha} \hat{\varphi}_{r\beta} - \varphi_{r\beta} \hat{\varphi}_{r\alpha} \right) dt$$
(44)

To improve the precision amounts adding a proportional gain to the integral action  $(K_p, K_i)$ .

$$\hat{\omega} = K_p \left( \varphi_{r\alpha} \hat{\varphi}_{r\beta} - \varphi_{r\beta} \hat{\varphi}_{r\alpha} \right) + K_i \int \left( \varphi_{r\alpha} \hat{\varphi}_{r\beta} - \varphi_{r\beta} \hat{\varphi}_{r\alpha} \right) dt .$$

According to equation (42) and (44), we can see that the estimated resistance depends on the estimated flux, therefore, it is not possible to obtain correct simultaneous speed and rotor resistance estimation.

In order to overcome this problem and to obtain simultaneous  $\hat{\omega}$  and  $\hat{R}_r$ , estimation, a small initial value is added to the estimated rotor flux. Once the estimate is obtained, we disable this value.

$$\hat{R}_r = R_r \frac{\hat{\varphi}_r}{\varphi_r} + R_0 \tag{45}$$

The block diagram of speed sensorless field-oriented using the new approach MRAS is presented in Fig. 2.

## 6 Type-2 Fuzzy Adapter

## 6.1 Interval type-2 Fuzzy

The interval type-2 fuzzy logic is depicted in Fig. 3. We discuss briefly the operation of each component of the FLC, with emphasis on type-reduction.

## • Fuzzifier

The fuzzifier maps a crisp input into the interval type-2 membership functions to produce a set of interval type-1 fuzzy sets. The number of sets depends on the number of inputs and membership functions. Singleton fuzzification was chosen due to its facility of implementation. Using singleton fuzzification two membership values are calculated for each fuzzy set i.e. the lower ( $\mu$ ) and upper ( $\bar{\mu}$ ) membership values.

## • Inference Engine

As in type-1 fuzzy logic, the inference is the logical operation by which a proposition is admitted by virtue of its liaison with other propositions held to be true. Only in type-2 fuzzy logic is used the type-2 fuzzy base rule. To carry out a relation between an input vector  $x = \{x_1, x_2, ..., x_p\}$  and the output (y), the activation



Fig. 2 Sensorless field-oriented control scheme.

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interval associated with the first outputs fuzzy set is calculated by the following equation:

$$\prod_{i=1}^{p} \mu_{\tilde{f}_{i}^{i}}(x_{i})$$
(46)

where  $\mu_{\tilde{j}_i^l}(x_i)$  is the activation interval associated with the variable  $x_i$ .

The fuzzy set of the output corresponding to the first rule is computed using the t-norm operator  $(\cap)$  as follows:

$$\mu_{\tilde{B}^{l}}(y) = \mu_{\tilde{G}^{l}}(y) \cap \left[\prod_{i=1}^{p} \mu_{\tilde{F}^{l}_{i}}(x_{i})\right]$$
(47)

Since only the interval type-2 fuzzy logic sets are used and the t-standard-product operation is implemented, then the activation interval associated with the first set of output defined by:

$$F^{i}(x) = [f_{\inf}^{i}(x), f_{\sup}^{i}(x)]$$
(48)

$$f_{\inf}^{i}(x) = \mu_{\tilde{F}_{1}^{i}\inf}(x_{1}) * \mu_{\tilde{F}_{2}^{i}\inf}(x_{2}) * \dots * \mu_{\tilde{F}_{p}^{i}\inf}(x_{p})$$
(49)

$$f_{\sup}^{i}(x) = \mu_{\tilde{F}_{1}^{i}\sup}(x_{1}) * \mu_{\tilde{F}_{2}^{i}\sup}(x_{2}) * \dots * \mu_{\tilde{F}_{p}^{i}\sup}(x_{p})$$
(50)

The terms  $\mu_{\tilde{F}_{p}^{i} \inf}(x_{i})$  and  $\mu_{F_{p}^{i} \sup}(x_{i})$  are respectively the lower and upper values of the interval activation corresponding to  $\mu_{\tilde{F}_{p}^{i}}(x_{p})$ .

## • Rules

The difference between the rules of a type-1 fuzzy logic system and those of type-2 will reside only in the nature of membership functions, therefore, the rules structure in the case of type-2 remains exactly the same as that of type-1, The only difference being that some membership functions will be type-2, Then the *i*-th rule of a type-2 fuzzy system will have the following form [23-26]:

IF 
$$x_1$$
 is  $\tilde{F}_1^i$  and  $x_2$  is  $\tilde{F}_2^i$  ...  $x_p$  is  $\tilde{F}_p^i$  THEN y is  $\tilde{G}^i$  (51)

Generally, the fuzzy rules are organized using tables which objective is to represent all the different combinations among the inputs of the system. The structure of the rule-base does not vary between type-1 and type-2 fuzzy logic.

#### • Type Reducer

Type-reduction translates the type-2 output sets of the



Fig. 3 Type-2 fuzzy Logic system Structure.

inference engine to a type-1 set; this is called a type reduced set. These type-reduced sets are then defuzzified to obtain a crisp output used for control.

We will use the "center-of-sets" type reduction, as it has reasonable computational complexity lying between Computationally expensive centroid type-reduction and the simple height and modified height type-reductions which have problems when only one rule fires. The type reduced set using the "center-of-sets" type-reduction is expressed below [23]:

$$Y(Z^{1}, Z^{2}, ..., Z^{M}, W^{1}, ..., W^{M}) = \int_{z^{1}} ... \int_{w^{1}} ... \int_{w^{1}} ... \int_{w^{M}} \frac{1}{\sum_{i=1}^{M} w^{i} z^{i}}{\sum_{i=1}^{M} w^{i}}$$
(52)

...

Since each set in (52) is a fuzzy set (type-1 interval), then (Y) is also a fuzzy set (interval type-1) that is the domain is located on the real axis:

$$Y(Z^{1}, Z^{2}, ..., Z^{M}, W^{1}, ..., W^{M}) = [y_{l}, y_{r}]$$
(53)

where, the type reduced set *Y* is an interval set defined by its left and right most points  $y_1$ ,  $y_r$ ,  $z^i = [z_{inf}^i, z_{sup}^i]$ ,  $w^i = [w_i^i, w_r^i]$  is the centroid of the type-2 interval consequent set  $\tilde{G}^i$ , whose details are given in [23], and i = 1, ..., M.

#### Defuzzifier

The defuzzification consists in transforming the typereduced fuzzy set into a crisp output. It is the simplest subsystem, the crisp output value is computed as the average of the bounds of the type-reduced set.

$$Y = \frac{y_l + y_r}{2} \tag{54}$$

with

$$y_{l} = \frac{\sum_{i=1}^{M} w_{l}^{i} z_{l}^{i}}{\sum_{i=1}^{M} w_{l}^{i}}, \quad y_{r} = \frac{\sum_{i=1}^{M} w_{r}^{i} z_{r}^{i}}{\sum_{i=1}^{M} w_{r}^{i}}$$
(55)

Using the Karnik-Mendel algorithm To calculate these two points [23, 24].

#### 6.2 Type-2 FLA Design of New Approach MRAS

The inputs of the adapter are the speed error and its variation. The adaptations made on the parameters of the PI regulator aim at correcting progressively the evolution of the system by acting on the regulation law. During the on-line operation of the regulator, a fuzzy matrix makes it possible to adapt the gains so as to optimize the characteristics of the temporal response. A rule base is designed, allowing as input variables e and  $\Delta e$  as output variables the variation rates  $K_1$  and  $K_2$  which must be added at each instant to the nominal

parameters  $K_{p_0}$  and  $K_{ip_0}$ , as shown in (58) and (59). The decision table is extracted from an expertise obtained following several simulation tests. Fig. 4 shows the structure of the adapter.

$$e = \omega_{\rm ref} - \hat{\omega} \tag{56}$$

$$\Delta e = \frac{de}{dt} \tag{57}$$

$$K_{p} = K_{1} + K_{p_{0}}$$
(58)

$$K_i = K_2 + K_{ip_0}$$
(59)

#### • Design of the Rule Base

To determine the basis of the rules, it is necessary to rely on considerations between the evolution of the PI parameters and the desired performance. To determine the basis of the rules, it is necessary to rely on considerations between the evolution of the parameters of the PI controller and the desired performance:

- > The integral gain  $K_i$  is increased, to improve the rise time during the transient regime, it is decreased as soon as the speed setpoint exceeds the tolerated zone in order to minimize the overshoot.
- The proportional gain K<sub>p</sub> is increased to reduce the rise time, except that this action increases the oscillations.
- > The variations on the proportional and integral gains have influences on the dynamics of the system which vary in the same direction. Depending on the position in the phase plane of e and  $\Delta e$ , it is necessary to recognize the positioning on the time curve and then to take action based on the abovementioned trends and on the objectives set in terms of performance. Thus we obtain the



## rules base illustrated by Table 1.

The membership functions of the input variables are shown in Fig. 5. Fig. 6 shows the general structure of a type-2 FLA, The only difference with type-1 is located at the output processing system.

## 7 Simulation and Experimental Results

The presented technique was initially verified using computer simulations. The simulations of the speed controlled FOC system with MRAS speed estimator and proposed  $R_r$  estimator are performed in MATLAB, Simulink Toolbox.

Fig. 20 shows the DSP based implementation of the speed sensorless IFOC control. The sampling frequency is fixed at 10kHz and the controller receives the stator currents measurements through two 8-bit A/D converters. Then, using the PWM technique, the reference voltages are sent to the machine via the voltage-source inverter whose switching frequency is fixed at 10kHz. Parameters of induction motor are  $R_s = 5.72\Omega$ ,  $R_s = 4.2\Omega$ ,  $L_s = L_r = 0.462$ H, M = 0.44H, J = 0.0049Kg.m<sup>2</sup>, f = 0.003NM/rad, p = 2.

#### 7.1 Simulation Results

The sensorless field-oriented control (FOC) induction motor drive, shown in Fig. 2, is used where the actual speed feedback signal is replaced by the estimated speed signal. Fig. 7 actual speed ( $\omega$ ), estimated speed ( $\hat{\omega}$ ) and reference speed ( $\omega_{ref}$ ). We see in Fig.8 that the tracking speed error ( $\omega_{ref} - \hat{\omega}$ ) is small even at zero speed regions and converge quickly to zero, also, in Fig.9 we can see that the speed estimation error  $(\omega - \hat{\omega})$  is acceptable. To test the robustness toward load torque for a speed reference. The step load of 5Nm is applied between t =4.2s and t = 7.2s, we can see, after very small variation of speed estimation error and speed tracking error, therefore, this disturbance does not affect system performance. We can see in Fig. 10 that the flux ( $\hat{\varphi}_{rd}$ ) installs correctly and the q-axis flux ( $\hat{\varphi}_{rq}$ ) is maintained at zero value, which confirms the field orientation.



All these results confirm the efficiency of our new approach observer and control. Fig.11 shows the direct and quadratic stator currents ( $i_{sd}$ ,  $i_{sq}$ ). Fig. 12 shows the correct estimate of the rotor resistance.

## 7.2 Experimental Results

Fig. 13 shows the performance of the speed estimation. This estimated speed is used in the new approach of the MRAS observer. We notice that the estimated speed is in agreement with the real speed.

Fig. 15 shows the flux  $\hat{\varphi}_{rd}$  is established correctly and follows the reference value, the quadric flux  $\hat{\varphi}_{rq}$  is practically nil, this confirms the vector control by decoupling. Fig. 18 shows that the tracking speed error is small and converges quickly to zero, also, in Fig. 17 we can see that the speed estimation error is very acceptable. Fig. 16 confirms the call of the current  $i_{sq}$  during the load application. Finally Fig. 19 .illustrates

the correct estimation of the rotor resistance  $\hat{R}_r$ .

All these Experimental results confirm the efficiency of the sensorless speed estimation for an induction motor (IM) based on the proposed observer.

## 8 Conclusion

This paper discusses the new approach MRAS (IS-MRAS) and rotor resistance estimation for speed sensorless control induction motor with on-line adaptation parameters. A novel adaptation mechanism using type-2 fuzzy logic controller, which replaces conventionally used PI controller in the adaptation mechanism. The speed estimation using the PI controller deteriorates at low speeds and hence proposed a T2FLC based speed observer that not only improves the performance during low speed but also makes the motor robust to external load torque disturbances. Simulation and experimental results show good performance of the



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**Fig. 19** Estimated rotor resistance  $\hat{R}_r$ .

sensorless control at low speed. Sensorless control of induction motor with on-line resistance estimation allows seeing the rotoric resistance variation in external load torque disturbances.





Fig. 16 Stator currents *isd* and *isq*.



Fig. 18 Tracking error.



Fig. 20 The experimental system in the L.T.I laboratory (University of Picardie, I.U.T of AISNE, 02880 CUFFIES) consisting of a 1.5kW induction motor, a voltage-source inverter, and a digital signal processor (DSP).

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